Genetic Algorithm Optimization of Log-Periodic Dipole Array

M. Touseef¹, Qamar-ud-Din², M. Aziz-ul-Haq¹, Umair Rafique¹, M. Arif Khan¹, M. Mansoor Ahmed¹

¹Department of Electronic Engineering, Mohammad Ali Jinnah University, Islamabad, 44000, Pakistan
²Department of Electrical Engineering, University of Faisalabad, Faisalabad, 38000, Pakistan

Abstract This paper presents Genetic Algorithm (GA) optimization of Log-Periodic Dipole Array (LPDA). Considering the fact that, an LPDA can effectively be used for different wireless communication systems such as WiMAX, GSM-I, GSM-II and WiFi, respectively. GA optimization is applied to the physical size of the antenna and on its gain. The proposed design is compared with the conventional LPDA design in terms of length, diameter and spacing between the dipole elements. Presented results show that, the proposed optimization approach can significantly improve the antenna gain and reduced its size. The size of the antenna is reduced up to 12% as compared to the conventional design. Also, the gain is improved from 9.1, 9.5, 9.2 and 8.5 dB to 10.7, 11.2, 9.9 and 9.1 dB for the desired communication bands. The reduction in size and increment in gain make LPDA an attractive choice for wireless applications.

Keywords Genetic Algorithm (GA), Log-Periodic Dipole Array (LPDA), Size Reduction, Cost Effective

1. Introduction

An antenna is a key component in any wireless communication system. These days, many wireless applications require high data rate at one hand, while small size of antenna on another hand. For this purpose, it is necessary to design such kind of antenna which is very efficient in terms of gain and occupy small space in the system. The goal of small size and high gain can be obtained using some optimization techniques such as Genetic Algorithm (GA)[1], Particle Swarm Optimization (PSO)[2] and its variants, e.g., Quantum PSO[3-6].

For broadband wireless applications, Log Periodic Dipole Array (LPDA) has been used since 1960s. The first LPDA design was introduced by[7-8] which later on had different designs for different applications. In general, an LPDA is a directional antenna which possesses constant electrical characteristics such as gain, impedance and front-to-back ratio over the wide range of frequencies compared to other directional antennas. The main advantage of an LPDA is that, it is essentially a frequency independent antenna for a certain multi-band communication system[9].

This paper presents the design of an LPDA which can operate at WiMAX, GSM-I, GSM-II and WiFi wireless communication bands. The main objective is to optimize the design using Genetic Algorithm (GA). However, there are other research works where GA is used to optimize different kind of antennas[1],[10-15]. In[1], authors used GA to find efficient new resonant wire antenna that perform best within the volume they are confined. In[10], authors used GA and Method of Moment (MoM) to compress the size of an LPDA in terms of its number of elements. However, in this work, we have optimized the overall size of the antenna. In[11], authors optimized an LPDA using GA, Nelder-Mead simplex algorithm and a combination of both algorithms.

The optimization problem presented in this paper has two objective functions. The design procedure is as follows: (1) First step is to design an LPDA using conventional technique and then analyse the response in terms of gain; (2) in the second step, we applied GA algorithm to optimize the antenna. The results of conventional design and the optimized design are discussed in Section 4.

The remainder of the paper is organized as follows. Section 2 explains the basics of Genetic Algorithm (GA). Section 3 discusses the design and optimization of an LPDA. Section 4 presents the results and discussion on results. Finally, we concluded the paper in Section 5.

2. Genetic Algorithm (GA)

Genetic Algorithm is based on the principle of best gene selection from a huge available population of genes. A portion of the worst population is rejected and the remaining population is arranged in a particular order. Two random selected best genes from the remaining population are allowed to mate and create a new population. After certain number of iterations, the available population, in general, is
the best population[16-17]. This principle of Genetic Algorithm is applied by different researchers on the antenna design[10-15].

Genes are the basic building blocks in any Genetic Algorithm technique. A gene is a binary encoding of a design parameter. Basically, chromosome is an array of genes. The chromosomes are evaluated by a function called cost function. The chromosomes are ranked from the most-fit to the least-fit and unacceptable chromosomes are discarded from the lower rank. Genes who survives become parents and by swapping some of their genetic material, new offspring is produced. The parents reproduce enough chromosomes to offset the discarded chromosomes. Thus, the total number of chromosomes remains constant in each iteration. The complete flow diagram of Genetic Algorithm is shown in Fig. 1.

**3. Design and Optimization of an LPDA**

A typical LPDA consists of a number of dipole elements \(L_i\), where, \(i = 1, \ldots, n\) showing that \(L_1\) and \(L_n\) are the largest and smallest elements mounted on a common feed network. The length, diameter and spacing of each element is different from the other elements. The schematic diagram of an LPDA is shown in Fig. 2. The smallest dipole element \(L_n\) is fed with a sinusoidal current of form \(i(t) = A\sin(\omega t)\) where, maximum value of \(i(t)\) is assumed to be unity. The step by step procedure of an LPDA is described in [18-20]. The basic design equations used to determine LPDA parameters are given below:

\[
\sigma = \frac{d_n}{2L_n} \quad (1)
\]

\[
L_{n+1} = L_n \times \tau \quad (2)
\]

\[
X_n = h_n \times \tan(\alpha) \quad (3)
\]

where

\[
\alpha = \tan^{-1}\left(\frac{1-\tau}{4\sigma}\right) \quad (4)
\]

where, \(\sigma, L, \alpha\) and \(X\) represents spacing factor, length, angle that bounds the dipole length, and spacing between \(L_1\) and \(L_n\) elements, respectively. The spacing between every two consecutive dipole elements is determined by using Eq. (1) where, spacing factor is defined as \(0.04 \leq \sigma \leq 0.22\). The length \(L_n\) of nth dipole element can be calculated by using Eq. (2) in which \(\tau\) is a scaling factor in the range \(0.76 \leq \tau \leq 1\). The distance from source to any dipole element is determined by using Eq. (4)[21].

The initial response of an LPDA is observed against the conventional design using \(\tau = 0.9, \sigma = 0.16, N = 10, L_n/d_n = 125\) and \(Z_0 = 50 \Omega\), respectively. The length of first dipole element is half of the wavelength such that \(L_1 = \lambda_{ref} \times 0.5\) where, \(\lambda_{ref}\) is calculated from reference frequency which is 400 MHz in our case. Also, the length of first dipole element can be calculated from the reference frequency. The rest of the lengths of each dipole element and other parameters are
calculated from the design equations. The response of an LPDA in terms of gain is calculated by using the procedure which discussed in [19].

An important factor in LPDA design is to determine the current across each dipole element. This current can be calculated by knowing the impedance \( Z_{ij} \) of each dipole element \( i \) with respect to other dipole element \( j \) and admittance \( Y_{ij} \) of the feeder line[19].

3.1. Implementation of GA

The first step in the algorithm implementation is to create a random population which consists of LPDA parameters such as length, diameter and spacing of each dipole element. In next step, we define a chromosome vector \( C \) which comprises of length (10 length genes), diameter (10 diameter genes) and spacing between two consecutive elements (9 spacing genes), respectively. Eq. (5) shows the chromosome vector \( C \). Our task is to optimize the define parameters in the chromosome vector.

\[
C = [L_1, L_2, ..., L_n, d_1, d_2, ..., d_n, X_1, X_2, ..., X_n] \quad (5)
\]

Chromosomes in the population are arranged in descending order on the basis of their cost. The lowest 50% of population is discarded and the best 50% are called parents. Two parents are randomly selected and mate. A random crossover point is selected and swaps both the parents from right hand side. As a result, new population is generated equal to the number of discarded population which is called off-spring. A small percentage from parents and off-spring is again discarded and new generation is searched. This new population is evaluated through a cost function which is given in eq. (6). The process is repeated until we obtain the best result. The cost function for the optimization process is given as:

\[
\text{Cost} = \frac{\sum_{f_H}^{f_I} \text{Gain}(f)}{f_H - f_I} \quad (6)
\]

where, \( f_H \) and \( f_I \) denotes the higher and lowest frequency bands. The cost function is designed to optimize the gain of an LPDA and it is also clear from Eq. (6). This cost function is compared with the initial gain at the end of each iteration. A condition is applied to check whether the gain is improved or not. All the optimized parameters of an LPDA against the improved gain are stored and shown in Table 1.

Table 1. Initial and optimized design of an LPDA

<table>
<thead>
<tr>
<th>Element</th>
<th>( L_n ) (m)</th>
<th>( d_n ) (m)</th>
<th>( X_n ) (m)</th>
<th>( L_n ) opt. (m)</th>
<th>( d_n ) opt. (m)</th>
<th>( X_n ) opt. (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.375</td>
<td>0.003</td>
<td>0.12</td>
<td>0.3675</td>
<td>0.0029</td>
<td>0.0975</td>
</tr>
<tr>
<td>2</td>
<td>0.3375</td>
<td>0.0027</td>
<td>0.108</td>
<td>0.3275</td>
<td>0.0026</td>
<td>0.0868</td>
</tr>
<tr>
<td>3</td>
<td>0.3038</td>
<td>0.0024</td>
<td>0.0972</td>
<td>0.2914</td>
<td>0.0023</td>
<td>0.0772</td>
</tr>
<tr>
<td>4</td>
<td>0.2734</td>
<td>0.0022</td>
<td>0.0875</td>
<td>0.2594</td>
<td>0.0021</td>
<td>0.0687</td>
</tr>
<tr>
<td>5</td>
<td>0.246</td>
<td>0.002</td>
<td>0.0787</td>
<td>0.2309</td>
<td>0.0018</td>
<td>0.0615</td>
</tr>
<tr>
<td>6</td>
<td>0.2214</td>
<td>0.0018</td>
<td>0.0709</td>
<td>0.2055</td>
<td>0.0016</td>
<td>0.0544</td>
</tr>
<tr>
<td>7</td>
<td>0.1993</td>
<td>0.0016</td>
<td>0.0638</td>
<td>0.1829</td>
<td>0.0015</td>
<td>0.0485</td>
</tr>
<tr>
<td>8</td>
<td>0.1794</td>
<td>0.0014</td>
<td>0.0574</td>
<td>0.1627</td>
<td>0.0013</td>
<td>0.0431</td>
</tr>
<tr>
<td>9</td>
<td>0.1614</td>
<td>0.0013</td>
<td>0.0517</td>
<td>0.1448</td>
<td>0.0012</td>
<td>0.0384</td>
</tr>
<tr>
<td>10</td>
<td>0.1453</td>
<td>0.0012</td>
<td>0.0465</td>
<td>0.1289</td>
<td>0.001</td>
<td>0.0234</td>
</tr>
</tbody>
</table>

4. Results and Discussion

This section presents the results of the proposed LPDA design. The main objective was to optimize an LPDA in such a way that, it works well in the desired frequency bands with the acceptable parameters which are physical size of an LPDA and its gain. The initial response is obtained by evaluating the design parameters and writing a MATLAB routine. The initial gain for different communication bands is shown in Fig. 3-6. After that, GA optimization is applied to the design parameters and the improvement in the gain is demonstrated. The results for the optimized design are shown in Fig. 3-6. These results show considerable improvement as compared to the conventional design. The gain is improved up to 85% for WiMAX band, approximately 85% for GSM-I, 93% for GSM-II and 93.5% for WiFi band, respectively. It is demonstrated that the proposed algorithm results are approximately similar to the previously presented work[2]. The major improvement in gain is noticed for WiMAX, GSM-I and GSM-II frequency bands as compared to the previous work[2]. The comparison of previous work with the proposed work is shown in Fig. 3-6. Also, the difference noticed in the computational time that, Genetic Algorithm (GA) optimization took less time to evaluate the parameters as compared to the Particle Swarm Optimization (PSO) and Quantum Particle Swarm Optimization (QPSO).

Figure 3. Initial and optimized gain for WiMAX

Figure 4. Initial and optimized gain for GSM-I
It is also observed that, the overall antenna size is reduced from 0.57m to 0.502m which is approximately 12% reduction in size. Table 1 shows the initial and optimized design parameters for the proposed LPDA.

5. Conclusions

The Log Periodic Dipole Array (LPDA) is designed for WiMAX, GSM-I, GSM-II and WiFi communication bands. Antenna parameters are optimized by using Genetic Algorithm (GA). The initial calculated average gain for each communication band is 9.1 dB, 9.5 dB, 9.2 dB and 8.5 dB, respectively. However, the optimum solution of average gain is 10.7 dB, 11.2 dB, 9.9 dB and 9.1 dB, respectively. It is also observed that the reduction occurred in the antenna size is 12% as compared to the initial design. With smaller size and high gain, the proposed design is an attractive choice for many wireless applications.

REFERENCES


