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1 **Development of a water quality index model - a**
2 **comparative analysis of various weighting methods**

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15 **Abstract.** The Water Quality Index (WQI) model is a popular tool for the assess-
16 ment of water quality (WQ) and its status classification. Over the last 50 years,
17 many different WQI models have been developed; while the four-component
18 structure remains common across the models, they vary in approaches in terms
19 of parameter selection and their associated weightings, and the methods used for
20 sub-indexing and aggregation. In this research, the parameter weight factors are
21 investigated. The parameters are assigned weightings depending on their signifi-
22 cance to the assessment. Recent research has revealed that that the WQI models
23 generate a significant amount of uncertainty as a result of this process. Most of
24 the WQI models widely used the expert opinion or analytical hierarchy process
25 (AHP) to estimate the parameters' weight values. Many researchers have argued
26 that these methods do not accurately represent the importance of parameters.

27 The aim of this study is to compare various statistical weighting approaches and
28 propose the most accurate method for calculating weight values in terms of un-
29 certainty. To estimate the weight value of parameters, four statistical attribute
30 weighting methods were used: (i) rank sum (RS), (ii) rank reciprocal (RR), (iii)
31 rank order centroid (ROC), and (iv) equivalent (EQ). In this study, the Guide to
32 the Expression of Measurement Uncertainty (GUM) approach was used to quan-
33 tify uncertainty of the weighting process by implementing Monte Carlo simula-
34 tion (MCS) technique. The finding of this study show that the ROC method pro-
35 duces the highest uncertainty, while the RS and EQ methods generate relatively
36 lower uncertainties. In terms of uncertainty, the results suggest that the rank sum
37 method is an effective method to estimate the weight value in developing a WQI
38 model.

39 **Keywords:** Water Quality Index Model; Monte Carlo simulation; Weight Val-
40 ues; Weighting Methods; Uncertainty; Random Forest, Rating Methods

41 **1 Introduction**

42 Water quality index (WQI) model is a popular tool due to its simple architecture and
 43 easy to application. Commonly, an ideal WQI model comprises including four compo-
 44 nents: (i) parameter selection, (ii) sub-index process, (iii) parameter weighting and (iv)
 45 aggregation function. This model is becoming increasingly popular and utilized to as-
 46 sess and classify water quality. Nevertheless, recent research has revealed that WQI has
 47 uncertainty problems in different stages [1-2]. The weighting technique is one of them.
 48 The present WQI used a variety of methods (such as expert opinions, analytical hierar-
 49 chy process, literatures) for generating parameters weight values. These methods have
 50 received much criticism due to its reliability in terms of uncertainty.

51 The present study have been carried out using amalgamation approaches with ma-
 52 chine-learning (ML) and multi-attributes (MA) statistical techniques. This approach
 53 was implemented by following two sequential steps. The first step of this process was
 54 to obtain the water quality rank for assigning degree of significant, then parameters
 55 weight values were estimated using four common rank-based weighting methods.

56 However, the purpose of this study is to explore an effective weighting method in
 57 order to reduce model uncertainty in developing a WQI model.

58 **2 Materials and Methods**

59 **2.1 Data Description**

60 For this study, data on water quality obtained from <https://www.catchments.ie/data/>.
 61 The Irish Environmental Protection Agency (EPA) has been collecting water quality
 62 data from 32 different monitoring sites in the Cork harbour in 2020 that was used in the
 63 current research as a case study. This study used the average concentration of water
 64 quality data from eleven parameters: ammonia (AMN), biological oxygen demand
 65 (BOD), dissolved oxygen (DO), chlorophyll a (CHL), molybdate reactive phosphorus
 66 (MRP), water pH, total organic carbon (TOC), total organic nitrogen (TON), water
 67 transparency (TRAN), dissolved inorganic nitrogen (DIN), and water temperature
 68 (TEMP)

69 **2.2 Parameters ranking procedures**

70 In this research, we conducted a study using ten widely used machine-learning (ML)
 71 algorithms for ranking water quality parameters based on their real-time relative im-
 72 portance. For ranking, this study utilized surface water quality guidelines that adopted
 73 by the Environmental Protection Agency (EPA) of Ireland. The random forest (RF)
 74 algorithm was found to be the most efficient for assigning parameter rankings [3]. In
 75 this research, the RF is used in order to provide the rank of water quality parameters.
 76 The RF prediction function defined as follows:

$$77 \quad f(x) = \sum_{m=1}^M c_m \prod (x, R_m) \quad (1)$$

78 where M denotes the number of regions in the features space, R_m is the region that
79 corresponds to m , c_m is a constant that relates to m .

$$80 \quad \prod (x, R_m) = \begin{cases} 1, & \text{if } x \in R_m \\ 0, & \text{otherwise} \end{cases} \quad (2)$$

81 The Gini scores are obtained by voting scores of each decision tree. Finally, the im-
82 portant features are chosen from the new subset based on the Gini score of the features
83 [3].

84 2.3 Estimating parameters weight values

85 The present study was used the four direct rating subjective methods to estimate weight
86 value of water quality parameters. These methods may avoid the problems highlighted
87 by recent studies. These functions are defined as follow:

$$88 \quad \text{(i) Rank Sum (RS) method: } w_i = \frac{n+1-i}{\sum_{j=1}^n j} = \frac{2(n+1-i)}{n(n+1)}, i = 1, 2, 3 \dots \dots, n \quad (3)$$

$$89 \quad \text{(ii) Rank Reciprocal (RR) method: } w_i = \frac{1/i}{\sum_{j=1}^n 1/j}, i = 1, 2, 3 \dots \dots, n \quad (4)$$

$$90 \quad \text{(iii) Rank Order Centroid (ROC) method: } w_i = \frac{1}{n} \cdot \sum_{j=1}^n \frac{1}{j}, i = 1, 2, 3 \dots \dots, n \quad (5)$$

$$91 \quad \text{(iv) Equal Weight (EQ) method: } w_i = \frac{1}{n}, i = 1, 2, 3 \dots \dots, n \quad (6)$$

92 where, n is the total number of attributes; i is the i^{th} attribute rank; j is the summation
93 of rank and w is the weight value.

94 The present study was used Monte Carlo simulation (MCS) approaches by following
95 the Guide to the Expression of Measurement Uncertainty (GUM) method to calculate
96 uncertainties in different weighting methods. In this study, the MCS run 103 trials for
97 MC simulation.

98 3 Results

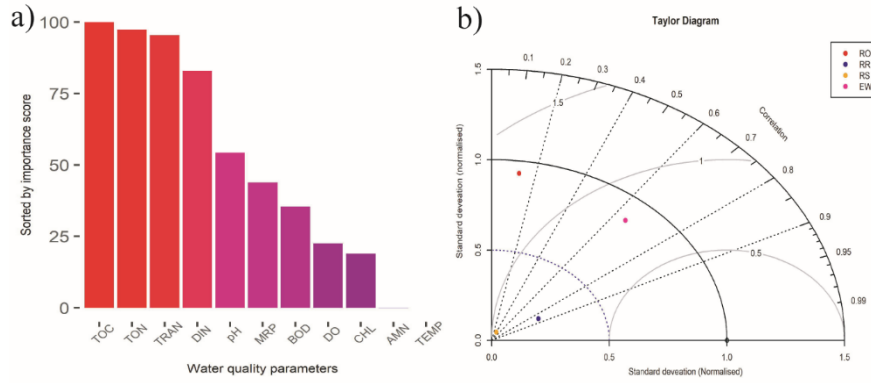
99 3.1 Ranks of water quality parameters

100 Figure 1 presents the rank of different water quality parameters were obtained from the
101 RF method. The results showed that the TOC, TON, TRAN and DIN are most im-
102 portant parameters in terms of water quality standards. AMN and temperature were
103 found to have no significance in the analysis of water quality for this study.

104 3.2 Comparative analysis of weighting methods

105 In this study, parameter weight values were estimated using four weighting methods.
106 In terms of weight variability of parameter, there was a significant difference between
107 the four weighting methods. Table 1 shows the weight values of different water quality
108 variables for different techniques respectively.

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Fig. 1. (a) Importance of water quality parameters; and (b) Cross-validation of the four weighting methods using Taylor diagram.

Table 1. Estimating weight values of water quality parameters.

WQ parameters	Rank	ROC	RR	RS	EW
TOC	1	0.4083	0.4082	0.2857	0.1667
TON	2	0.2417	0.2041	0.2381	0.1667
TRAN	3	0.1583	0.1361	0.1905	0.1667
DIN	4	0.1028	0.1020	0.1429	0.1667
pH	5	0.0611	0.0816	0.0952	0.1667
MRP	6	0.0278	0.0680	0.0476	0.1667

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3.3 Uncertainty analysis

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The current study investigated into a significant difference in weight variation of water quality parameters between weighting methods. Table 2 shows the summary statistics of probability distributions of ROC, RR, and RS weighting methods were triangular and EW method was normal distribution.

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Table 2. Different-weighting methods and related PDFs

Weighting methods	PDFs	PDF parameters
ROC	Triangular	$a = 0.0278$; $b = 0.4083$; $c = 0.16667$
RR	Triangular	$a = 0.0680$; $b = 0.4082$; $c = 0.16667$
RS	Triangular	$a = 0.0476$; $b = 0.2857$; $c = 0.16667$
EW	Normal	Mean = 0.1667; SD = 0.00

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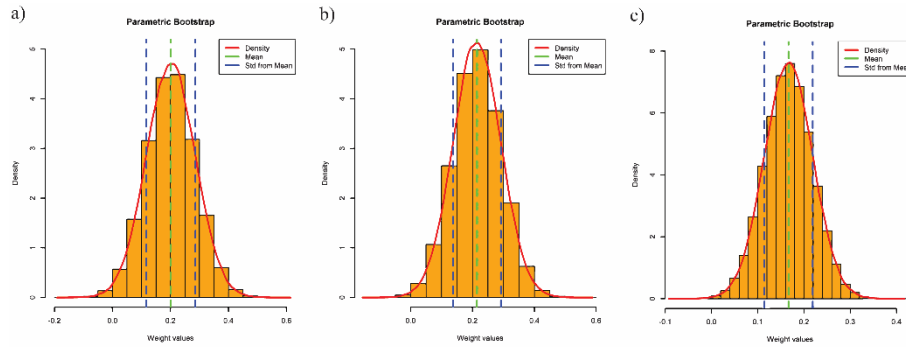
As seen in Figure 2, it shows the summary of MCS results. Table 3 provides comparative statistical scenarios between various weighting procedures. According to MCS results, the ROC method produced the highest weighting uncertainty, while the RS method produced the lowest. Table 4 presents the uncertainty results obtained from the MCS analysis for different weighting methods.

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128 **Table 3.** Descriptive statistics of different weighting techniques.

Ranking methods	Descriptive statistics				
	Minimum	Maximum	Mean	SE	Std.
ROC	0.0278	0.4083	0.1667	0.0573	0.1404
RR	0.0680	0.4082	0.1667	0.0522	0.1279
RS	0.0476	0.2857	0.1667	0.0364	0.0891
EQ	0.1667	0.1667	0.1667	0.0000	0.000

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Fig. 2. Density plots for input PDFs of water quality parameters obtained from by MCS method: (a) ROC; (b) RR; (c) RS

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Table 4. Uncertainty with 95% coverage probability of different weighting methods.

Ranking methods	Uncertainty parameters			
	SU ¹	EDF ²	CF ³	EU ⁴
ROC	0.0320	5	2.57	0.0823
RR	0.0292	5	2.57	0.0751
RS	0.0198	5	2.57	0.0509
EQ	0.0	5	2.57	0.0

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3.4 Cross-validation of uncertainty results

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The effectiveness of the methods was compared and visualized using a Tylor diagram. The correlation coefficient (R), root mean square difference (RMSD), and standard deviation (SD) between any prediction and observation weight values are shown in this diagram. The RS method, as shown in Figure 1b, falls into lines with the lowest RMSD and SD between predicted and observed weighted values. The findings suggest that the RS method could help improve the weighting system's accuracy.

142 4 Discussion

143 As mentioned in the recent research, the weighting method contributes to the uncer-
144 tainty in the WQI model. Six water quality parameters out of eleven were found to be
145 significant in the current study in order to assess water quality in Cork Harbour, Ireland.
146 The finding confirms that different weighting methods resulted in significant differ-
147 ences in parameter weight values. Figure 1b shows the summary statistics for different
148 weighting methods. In contrast to four weighting methods, different methods show sig-
149 nificant variation, which is consistent with previous literature. From the figure 1b, it
150 can be seen that the RS method produced the lowest uncertainty relatively the highest
151 weight variation was produced by ROC methods. However, recent research has re-
152 vealed that the rank order centroid (ROC) weights lead to the highest performance in
153 identifying the best alternative under the ranked attribute weights due to its sharpness
154 and non- linear function. The findings of this study suggest that the rank sum method
155 is an effective technique for estimating weight value in developing a WQI model.

156 5 Conclusions

157 The present study examined the performance of four statistical weighting methods in
158 order to estimate weight values of water quality parameters. In terms of contribution to
159 uncertainty in WQI model, the results indicate that the rank sum method is robust
160 method to estimate the weight value than other methods. This new study could aid in
161 reducing uncertainty and improving the WQI model's performance. The present study
162 has confirmed the finding of recent studies, which revealed that the weighting method
163 contributes to the uncertainty in WQI model. Therefore, according to analysis the
164 weighting values had a slight significant impact on producing uncertainty in WQI
165 model. Statistically, it could be held statistically accountable to estimate weight values
166 in the WQI model due to this study was calculated less than two percent uncertainty in
167 weighting process.

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